



iii)  $\frac{\partial}{\partial x} (x^y) =$

- a) 1    b)  $yx^y$   
c)  $x^y \log x$     d)  $yx^{y-1}$ .

iv) If  $P = \{ 2, 4, 6, 7, 8, 9 \}$ ,  $Q = \{ 1, 2, 6, 9 \}$  then  $P \cap Q$  is

- a)  $\{ 1, 2, 6 \}$     b)  $\{ 2, 6, 9 \}$   
c)  $\{ 1, 6, 9 \}$     d)  $\{ 4, 6, 9 \}$ .

v) The value of  $\lim_{x \rightarrow 3} \frac{x^3 - 3^3}{x - 3}$  is

- a) - 12    b) 12  
c) 27    d) - 27.

vi) If  $A$  be a matrix whose inverse exists then which of the following is not true ?

- a)  $(A^T)^{-1} = (A^{-1})^T$   
b)  $A^{-1} = (\det(A))^{-1}$   
c)  $(A^2)^{-1} = (A^{-1})^2$   
d) none of these.

- vii) The equation  $x^4 + 2x^2 - 7x - 5 = 0$  has
- one real roots and three complex roots
  - one complex roots and three real roots
  - two real roots and two complex roots
  - four real roots.
- viii) Cardan's method is used for solving equation of degree
- 2
  - 3
  - 4
  - none of these.
- ix) If  $\alpha, \beta, \gamma$  be the roots of  $x^3 - 3x^2 + 6x - 2 = 0$ , then  $\sum \alpha\beta$  is
- 3
  - 6
  - 2
  - none of these.
- x)  $f(x, y) = \sqrt{x} + \sqrt{y}$  is a function of degree
- $\frac{1}{2}$
  - $\frac{1}{3}$
  - 0
  - $\frac{1}{4}$ .

xi) The equation  $r = 3 \sin \theta + 4 \cos \theta$  represents

- a) a parabola                      b) an ellipse  
c) a straight line                  d) a circle.

xii) The inverse of the matrix  $\begin{bmatrix} 2 & 3 \\ 4 & 6 \end{bmatrix}$  is

- a)  $\begin{bmatrix} 2 & -3 \\ 4 & 6 \end{bmatrix}$                       b)  $\begin{bmatrix} 1 & 2 \\ -\frac{3}{2} & 3 \end{bmatrix}$   
c)  $\begin{bmatrix} -2 & 4 \\ -3 & 6 \end{bmatrix}$                       d) does not exist.

**GROUP - B**

**( Short Answer Type Questions )**

Answer any *three* of the following.                   $3 \times 5 = 15$

2. Prove that the set of real numbers of the form  $a + b \sqrt{2}$  where  $a$  and  $b$  are rational numbers, forms a field under addition and multiplication.
3. Solve the equation  $x^3 - 9x^2 + 14x + 24 = 0$ , two of whose roots are in the ratio 3 : 2.
4. Prove that, any square matrix can be expressed as the sum of a symmetric matrix and a skew-symmetric matrix.

5. If  $u = \tan^{-1} \left( \frac{x+y}{\sqrt{x} + \sqrt{y}} \right)$ , then show that

$$x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \frac{1}{4} \sin 2u.$$

6. A function  $f(x)$  is defined as follows

$$\begin{aligned} f(x) &= 1 + x \text{ when } x \leq 2, \\ &= 5 - x \text{ when } x > 2. \end{aligned}$$

Show that  $f(x)$  is continuous at  $x = 2$  but  $f'(2)$  does not exist.

### GROUP - C

#### ( Long Answer Type Questions )

Answer any *three* of the following.  $3 \times 15 = 45$

7. a) State Descart's rule of sign. Using this rule find the nature of the roots of the equation

$$x^4 - 7x^3 + 21x^2 - 9x + 21 = 0.$$

- b) Solve the following system of linear equations by Cramer's rule

$$x - y + 2z = 1$$

$$x + y + z = 2$$

$$2x - y + z = 5.$$

- c) If by a transformation of one rectangular axis to another with same origin the expression  $ax + by$  changes to  $a'x' + b'y'$ , Prove that  $a^2 + b^2 = a'^2 + b'^2$ .

8. a) Show that the equation  $20x^2 + 15xy + 9x + 3y + 1 = 0$  represents a pair of intersecting straight lines which are equidistant from the origin.

b) Show that  $\cos x > 1 - \frac{x^2}{2}$  if  $0 < x < \frac{\pi}{2}$ .

c) If  $\alpha, \beta, \gamma$  be the roots of the equation

$$x^3 - px^2 + qx - r = 0, \text{ then find the value of } \sum \frac{1}{\alpha}.$$

9. a) If  $A = \{a, b, c, d, e\}$ ,  $B = \{c, a, e, g\}$  and  $C = \{b, e, f, g\}$ ,

$$\text{then show that } (A \cup B) \cap C = (A \cap C) \cup (B \cap C).$$

b) Reduce the following equation to the canonical form and determine the nature of the conic represented by it

$$x^2 - 4xy + 4y^2 - 12x - 6y - 39 = 0.$$

c) Evaluate  $\lim_{x \rightarrow 1} \left( \frac{x}{x-1} - \frac{1}{\log x} \right)$ .

10. a) Evaluate  $\int \frac{dx}{(1+x)\sqrt{1-x^2}}$ .
- b) If PSQ be a focal chord of a conic with focus  $S$  and semi-latus rectum  $l$ , then prove that  $\frac{1}{SP} + \frac{1}{SQ} = \frac{2}{l}$ .
- c) If  $A - 2B = \begin{bmatrix} 0 & 6 & 26 \\ 6 & -9 & 12 \\ 2 & 9 & -10 \end{bmatrix}$  and
- $$2A + B = \begin{bmatrix} 10 & -3 & 4 \\ 12 & -3 & 4 \\ 4 & 3 & 0 \end{bmatrix}, \text{ find } A \text{ and } B.$$
11. a) If  $G$  be a group such that  $(ab)^2 = a^2b^2 \forall a, b \in G$ , show that the group  $G$  is abelian.
- b) Show that  $\int_0^1 \frac{\log(1+x)}{1+x^2} dx = \frac{\pi}{8} \log 2$ .
- c) If  $y = e^{-x} \sin x$ , then show that  $y_4 + 4y = 0$ .

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